

Note on Homological Mirror symmetry

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Abstract

This is a note for the seminar on Calabi-Yau manifolds in string theory beginning in spring 2023. The basic goal of this seminar is to reach Homological Mirror Symmetry (HMS).

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